

Simposio Internacional sobre Sistemas de Emisarios 2023 International Symposium on Outfall Systems 2023

# Comparison between Eulerian and Lagrangian approaches to pollutant transport modelling in shallow coastal waters

**ISOS**|2023

AUTHORS: NATHAN P. A. V. DA COSTA <sup>A,\*</sup>, TOBIAS BLENINGER <sup>A</sup>, MAURÍCIO F. GOBBI <sup>A</sup> AND SILENE C. <u>BAPT</u>ISTELLI <sup>B</sup>





#### **INTRODUCTION**



#### **INTRODUCTION**











#### **METHODOLOGY - HYDRODYNAMICS**

#### Model characteristics:

- 2DH model
- Low stratification of water column
- Shallow waters transient equations
- Hydrostatic distribution of pressure
- Incompressible flow
- Boussinesq hypotesis
- κ-ε closure scheme
- Astronomical ocean data used for open boundary condition

#### Model forcings:

Initial conditions:

- Wind
- Temperature

nternational Association or Hydro-Environment

ring and Researc

Salinity

- Water level = 0 m
- Temperature = 25.68 °C
- Salinity = 35.28 ppt





#### **METHODOLOGY - EULERIAN VS. LAGRANGEAN (DELFT3D – WAQ/PART)**

Advection + Diffusion + Reaction governing equation:

$$\frac{\partial C}{\partial t} + v_x \frac{\partial C}{\partial x} - D_x \frac{\partial^2 C}{\partial x^2} + v_y \frac{\partial C}{\partial y} - D_y \frac{\partial^2 C}{\partial y^2} + v_z \frac{\partial C}{\partial z} - D_z \frac{\partial^2 C}{\partial z^2} = S + f_R(C, t)$$



Initial condition:

- Background concentration of analyzed parameters = 0
- Dissolved oxygen = 8 mg L<sup>-1</sup>

nternational Association

or Hydro-Environmen

- Main sources:
  - Ocean outfalls
- Streams and tributary channels

#### Model characteristics:

- Dynamic 3-D particle tracking model
- Horizontal and vertical dispersion coefficients treated separately
- Transport is split between
  - advection (currents and wind)

x

horizontal/vertical dispersion (random walk)



$$(t + \Delta t) = x(t) + \int_0^{\Delta t} \left(\frac{dx}{dt}\right) dt$$

$$D_{x,y} = at^{t}$$



#### **RESULTS – TRANSPORT PREVIW - FLOW (EULERIAN)**



Plume spread - FLOW



#### **RESULTS – EULERIAN (DELFT3D – WAQ) – E. COLI**



Mean (30 days) – Total coliforms – filter of 1000 NMP/100ml



Mean (30 days) – Enterococcus – filter of 100NMP/100ml



Mean (30 days) – Fecal coliforms – filter of 1000NMP/100ml





#### **RESULTS – EULERIAN (DELFT3D – WAQ) – STATISTICS**



#### **RESULTS – LAGRANGIAN (DELFT3D – PART) – PG3**

Plume spread







aysa

🗼 llega.

Ministerio de Obras Públicas Argentina

#### **RESULTS – LAGRANGIAN (DELFT3D – PART) – PG3 – E. COLI**



#### **RESULTS – LAGRANGIAN (DELFT3D – PART) – PG3 – TOTAL** COLIFORMS



#### **CONCLUDING REMARKS**

- Eulerian approach
  - Calibrated model
  - Varying decay rate of analyzed parameters
  - Closure model solved via k-e scheme
- Solves concentration via finite volume method, thus may cause numerical diffusion when dealing with elevated concentration gradients
- In the Eulerian scheme, the pollutant is diluted to a whole grid cell soon after being emitted from a point source so that the concentration is reduced instantaneously
- Provide information for the whole domain

- Lagrangian approach
  - Not calibrated model, thus results are thoroughly associated with the velocity field obtained from hydrodynamics
  - Constant minimum decay rate
- Solves concentration of the particle via decay rate, T90
- Virtually free of numerical diffusion
- The concentration of the pollutant is associated with a particle not the whole grid cell, thus if there are not enough particles the outcome may not be realistic
- Depends on the velocity field originated from an Eulerian hydrodynamic simulation





#### **CONCLUDING REMARKS**

- Preliminary results indicate:
  - Plume size and concentration for E. Coli parameter diverged sligthly between each one of the applied concepts
    - Lagrangian approach resulted in a less concentrated and smaller mean plume Adequate calibration of the model may result in a smaller sized and concentration plume
  - Enterococcus parameter maintained its pattern for both approaches
  - Similar overall dispersion pattern between both approaches





#### **TASKS FOR THE FUTURE**

- Simulate the remaining outfall systems as point-sources
- Apply varying decay rate for the analysed parameters
- Adequately calibrate the particle model
- Evaluate and compare the resulting plume from both approaches
- Simulate the ramaining outfall systems as nonpoint-sources
- Evaluate the effects of nonpoint-sources as a continuous discharge for the particle track model









## UNIVERSIDADE FEDERAL DO PARANÁ

### Thank you for your time!









#### Simposio Internacional sobre Sistemas de Emisarios 2023

International Symposium on Outfall Systems 2023

